

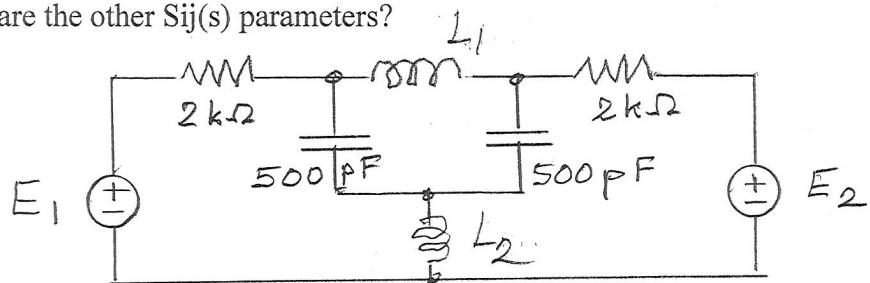
FINAL EXAMINATION
December 6, 2006, 12 - 1:50 pm

ECE 580
Prof. G.C. Temes

1. In the circuit shown, $S_{11}(s) = 0$ for all $s = j\omega$.

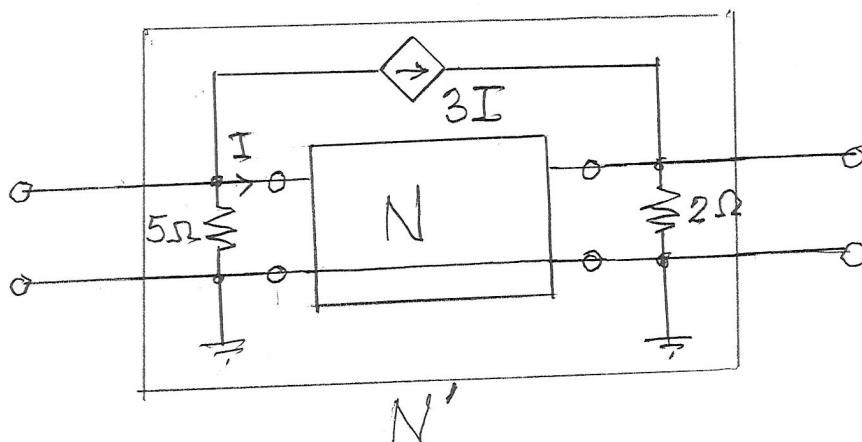
a. Find the missing element values.

b. What are the other $S_{ij}(s)$ parameters?



2. Find the adjoint of an ideal transformer. What is the change in the output voltage or current of a linear circuit containing it, if the turns ratio \underline{n} changes by Δn ?

3. Find the admittance matrix of the twoport N' . The admittance parameters of the embedded twoport N are $y_{11} = 2 \text{ S}$, $y_{12} = -4 \text{ S}$, $y_{21} = 8 \text{ S}$, and $y_{22} = 10 \text{ S}$.



1.a. For $I_1 = 1 \text{ A}$

$$V_1 = Z_1 = z_{11}I_1 + z_{12}I_2 = z_{11} - z_{12} V_2 / R$$

$$V_2 = z_{21}I_1 + z_{22}I_2 = z_{12} - z_{22} V_2 / R$$

$$V_2 = \frac{z_{12}}{1 + z_{22}/R}$$

$$Z_1 = z_{11} - \frac{z_{12}^2/R}{1 + z_{22}/R} = \frac{z_{11}R + \det Z}{R + z_{22}}$$

For $Z_1 = R$, $z_{11} = z_{22}$

$$R^2 + z_{11}/R = z_{11}R + z_{11}^2 - z_{12}^2$$

$$z_{11} = sL_2 + \frac{1}{sC} - \frac{1/sC}{s^2L_1C + 2}$$

$$z_{12} = sL_2 + \frac{1/sC}{s^2L_1C + 2}$$

$$(z_{11} + z_{12})(z_{11} - z_{12}) = (2sL_2 + \frac{1}{sC})(\frac{1}{sC} - \frac{2/sC}{s^2L_1C + 2})$$

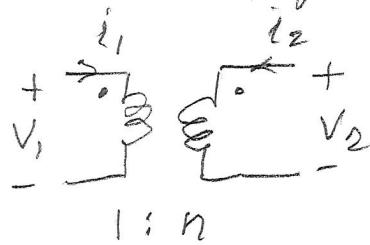
$$= \frac{L_1}{C} \frac{2s^2L_2C + 1}{s^2L_1C + 2} = R^2$$

$$2L_1L_2Cs^2 + L_1 = R^2L_1C^2s^2 + 2R^2C$$

$$L_1 = 2R^2C = 2 \times 4 \times 10^6 \times 5 \times 10^{-10} = 4 \mu\text{H}$$

$$L_2 = \frac{4 \times 10^6 \times 5 \times 10^{-10}}{2} = 1 \mu\text{H} = \frac{R^2C}{2}$$

2. Ideal transformer



$$\begin{aligned} V_2 &= nV_1 \\ i_1 &= -ni_2 \end{aligned} \quad \begin{bmatrix} V_2 \\ i_1 \end{bmatrix} = \begin{bmatrix} n & 0 \\ 0 & -n \end{bmatrix} \begin{bmatrix} V_1 \\ i_2 \end{bmatrix}$$

$$\underline{\underline{Y}} = \underline{\underline{H}} \underline{\underline{X}}$$

$$\Delta \underline{\underline{y}} \approx \underline{\underline{H}} \Delta \underline{\underline{x}} + \Delta \underline{\underline{H}} \underline{\underline{x}}$$

$$\underline{\underline{\hat{y}}} = \underline{\underline{\hat{H}}} \underline{\underline{\hat{x}}}$$

Branch
sews.

$$\hat{i}_1 \Delta V_1 - \hat{V}_1 \Delta i_1 + \hat{i}_2 \Delta V_2 - \hat{V}_2 \Delta i_2 =$$

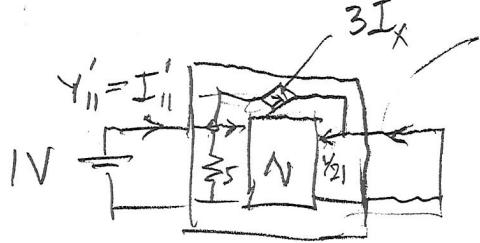
$$\Delta \underline{\underline{y}} = \hat{i}_1 \Delta V_1 - \hat{V}_1 (-n \hat{i}_2 - \Delta n \cdot \hat{i}_2) + \hat{i}_2 (\Delta n \cdot V_1 + n \cdot \Delta V_1) - \hat{V}_2 \Delta i_2$$

To eliminate ΔV_1 , $\hat{i}_1 = -n \hat{i}_2$] Same as
 $-n - \Delta i_2$, $n \hat{V}_1 = \hat{V}_2$] in N

Then, sews.

$$+ \hat{V}_1 \hat{i}_2 \Delta n + \hat{i}_2 V_1 \Delta n \rightarrow \frac{\partial \text{out}}{\partial n} = \hat{V}_1 \hat{i}_2 + \hat{i}_2 V_1$$

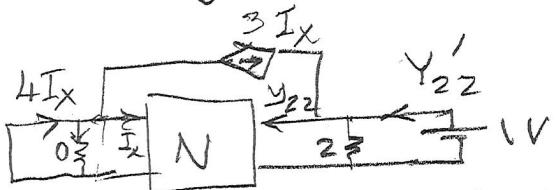
3.



$$I_1 = Y_{11}' V_1 + Y_{12}' V_2$$

$$I_2 = Y_{21}' V_1 + Y_{22}' V_2$$

$$Y_{11}' = I_{11}' = \frac{1}{5} + 2 + 6 = 8.2 \text{ S} \quad \checkmark$$



$$Y_{22}' = \frac{1}{2} - 3 \times \left(\frac{4}{4} \right) + 10 = 22.5 \text{ S} \quad \checkmark$$

$$I_1 = Y_{11} V_1 + Y_{12} V_2$$

$$Y_{12}' = 4 Y_{12} = -16 \text{ S} \quad \checkmark$$

$$I_2 = Y_{21} V_1$$

$$Y_{21}' = Y_{21} - 3 I_x = Y_{21} - 3 Y_{11} = 8 - 6 = 2 \text{ S} \quad \checkmark$$

$$\tilde{Y}' = \begin{bmatrix} 8.2 & -16 \\ 2 & 22.5 \end{bmatrix} \text{ S}$$